

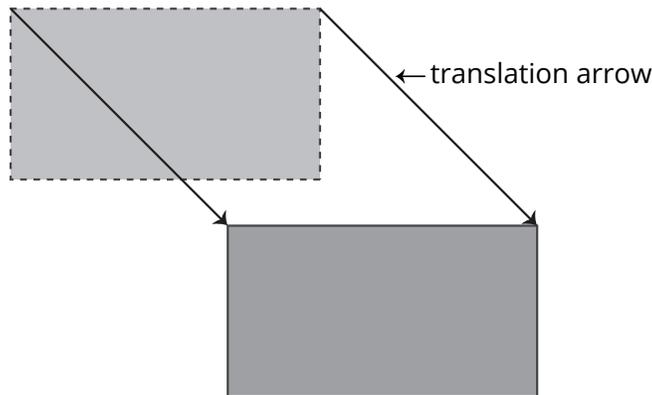
## 3 Combining Transformations

### Transformations

A change to a shape is called a transformation. Transformations include translations (slides), reflections (flips), and rotations (turns).

### Performing Translations

- A translation of a shape is a slide. A translation moves every point on the shape in the same direction and the same distance.
- A translation arrow connects a point on the original shape to where the shape moves. The translation arrow is the same for every point on the shape.



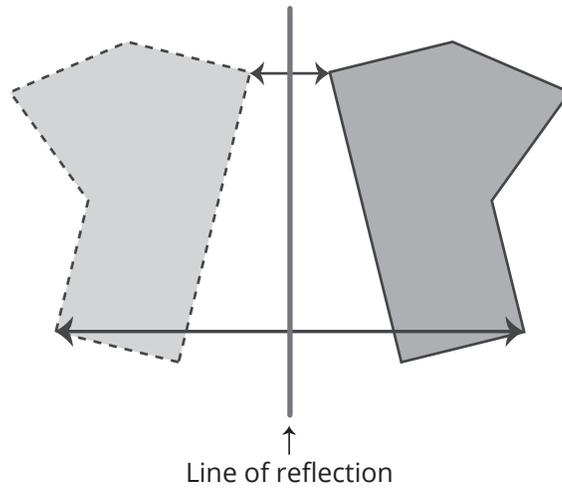
Translation arrows are the same for every point on a shape.

- A shape does not change in size, shape, or orientation when it is translated. Therefore, if you move the corners of a shape using the same translation arrow, you can draw lines joining the new positions to move the rest of the shape.

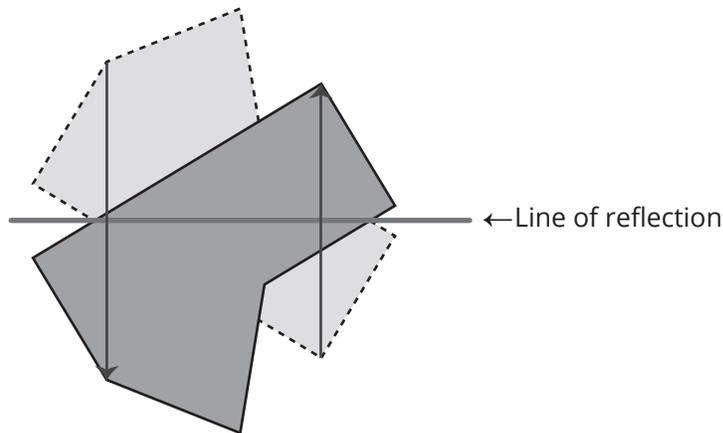
### Performing Reflections

- A reflection of a shape creates a mirror image of the shape. You can reflect a shape using a transparent mirror (such as a Mira) or another reflecting device.

The line joining any point on the original shape to its final location is at right angles to the line of reflection. Also, matching points are just as far away from the line of reflection on one side as they are on the other side.

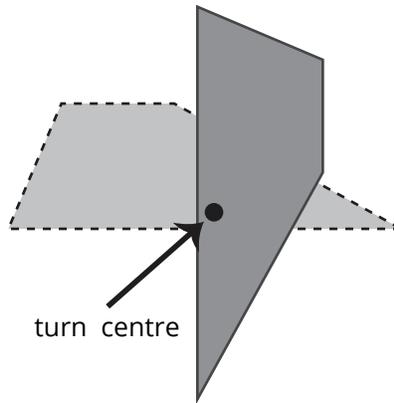


- The line of reflection can be outside the shape, as above, or inside the shape. If it is inside, you have to be careful to reflect both sides of the shape.

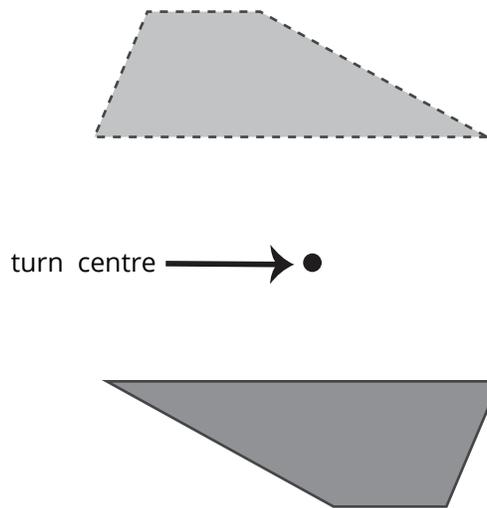


**Performing Rotations**

- A rotation turns a shape either clockwise or counterclockwise around a point called a turn centre. The turn centre can be inside or outside the shape.
- In Grade 6, students perform rotations of  $90^\circ$  and  $180^\circ$ , but nothing beyond that.



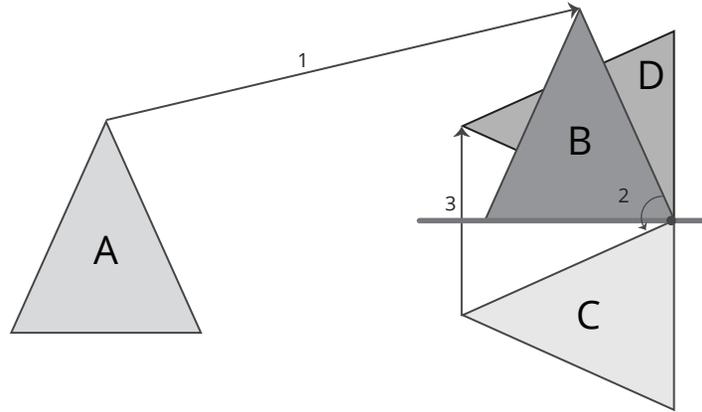
This trapezoid was rotated  $90^\circ$  clockwise about a turn centre inside the shape.



This trapezoid was rotated  $180^\circ$  about a turn centre outside the shape.

### Moving From One Shape to a Congruent Shape

- You can use a combination of translations, reflections, and/or rotations to move from any 2-D shape to an identical, congruent shape.



To move from **A** to **D**, you could:  
 1. translate to get to **B**,  
 2. rotate  $90^\circ$  counterclockwise to get to **C**, and then  
 3. reflect to get to **D**.

### Definitions

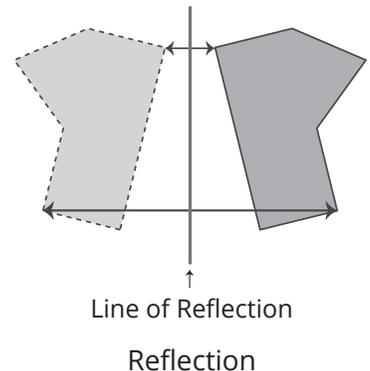
**clockwise:** the direction a clock's hands move

**congruent:** identical in shape and size

**counterclockwise:** the direction opposite to the way a clock's hands move

**line of reflection:** the line across which a shape is reflected or flipped

**reflection:** a transformation in which a shape is flipped across a line of reflection to form a mirror image without changing size or shape but with a change in orientation



**Definitions (continued)**

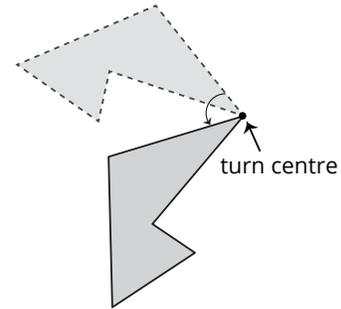
**rotation:** a transformation in which a shape turns about a stationary turn centre without changing size, shape, or orientation

**transformation:** a process that changes the position or orientation of a shape; for example, translation, reflection, rotation

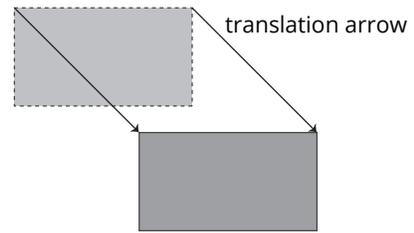
**translation:** a transformation in which a shape slides to a new position without changing size, shape, or orientation

**translation arrow:** an arrow connecting a point on a shape to where that point moves in a translation

**turn centre:** a stationary point that a shape is rotated about; the turn centre can be inside the shape, outside the shape, or on a vertex or side of the shape



Rotation



Translation